## **Berechne ohne Taschenrechner: 1)** $\frac{3}{5} + \frac{1}{8} + \frac{17}{20} + \frac{3}{4} + \frac{1}{2}$ **2)** $\frac{51}{16} - \frac{1}{8} - \frac{3}{4} - \frac{1}{2}$ **3)** $\frac{4}{7} + \frac{3}{28} + \frac{2}{3} - \frac{3}{4}$ **4)** $\frac{12}{7} + \frac{18}{72} - \frac{20}{36} - \frac{7}{12} + \frac{5}{6} - \frac{2}{3} + \frac{7}{9} - \frac{3}{8}$ **5)** $3\frac{1}{2} + 4\frac{3}{5} - 6\frac{11}{14} + \frac{29}{35} - \frac{9}{10} + 2\frac{29}{35} + 1\frac{3}{7}$ 7) $\frac{41}{118} \cdot \frac{59}{205}$ **6)** $\frac{432}{576} \cdot \frac{95}{133}$ **8)** $\frac{81}{243} \cdot \frac{27}{18}$ **9)** $\frac{32}{64} \cdot \frac{17}{49} \cdot \frac{13}{11} \cdot \frac{98}{17} \cdot \frac{22}{39} \cdot \frac{33}{77} \cdot \frac{16}{64}$ **10)** $\frac{45}{46} \cdot \frac{126}{414} \cdot \frac{23}{10} \cdot \frac{2317}{4011} \cdot \frac{4011}{2317} \cdot \frac{21}{27}$ **11)** $3\frac{3}{4} \cdot 4\frac{7}{9}$ **13)** $2\frac{1}{3} \cdot 5\frac{5}{6}$ **12)** $6\frac{4}{7} \cdot 5\frac{11}{23}$ **14)** $1\frac{8}{17} \cdot 1\frac{38}{117} \cdot 6\frac{4}{5} \cdot 1\frac{8}{31}$ **15)** $\frac{2}{3} : \frac{4}{5}$ **16)** $\frac{4}{5}:\frac{2}{3}$ **18)** $\left(\frac{12}{16}:\frac{54}{81}\right):\left(\frac{48}{114}:\frac{24}{798}\right)$ **17)** $\frac{9}{11}:\frac{36}{17}$ **19)** $\left(12\frac{1}{4}:\frac{7}{12}\right):\left(3\frac{5}{6}:7\frac{7}{27}\right)$ **20)** $\frac{29}{3} + \frac{4}{6}\cdot\frac{5}{10}\cdot\frac{125}{625} - \frac{103}{515}\cdot\frac{67}{31}\cdot\frac{62}{268}\right)$ **21)** $\left(4\frac{7}{12} - 2\frac{1}{6}\right) \cdot \left(3\frac{5}{9} - 2\frac{3}{4}\right) + \frac{39}{72} : 1\frac{5}{8}$ **22)** $\left(1\frac{2}{3}:4\frac{1}{2}\right)^3 + 7\frac{1}{4}\cdot 3\frac{5}{9} - 4\frac{17}{36} + \left(1\frac{1}{2}\right)^5$ **23)** $15\frac{2}{3} - \left| 6\frac{1}{2} \left( 2\frac{1}{4} - \frac{7}{8} \right) + \frac{3}{4} \right| : 6$ **24)** $\left(3\frac{1}{8} - 2\frac{3}{4}\right)^2 + \frac{5}{2} + \frac{3}{8} + \frac{1}{2}\left(\frac{3}{2} \cdot \frac{6}{8}\right)^2$ **25)** $12 \cdot 14 - 7\frac{1}{2} \cdot 5 + 6\frac{1}{3}\left(3 - \frac{1}{2}\right)^3$



## Lösungen

1)	$\frac{3}{5} + \frac{1}{8} + \frac{17}{20} + \frac{3}{4} + \frac{1}{2} = \frac{24}{40} + \frac{5}{40} + \frac{34}{40} + \frac{30}{40} + \frac{20}{40}$	=	$\frac{113}{40}$	=	$2\frac{33}{40}$
2)	$\frac{51}{16} - \frac{1}{8} - \frac{3}{4} - \frac{1}{2} = \frac{51}{16} - \frac{2}{16} - \frac{12}{16} - \frac{8}{16}$	=	<u>29</u> 16	=	$1\frac{13}{16}$
3)	$\frac{4}{7} + \frac{3}{28} + \frac{2}{3} - \frac{3}{4} = \frac{48}{84} + \frac{9}{84} + \frac{56}{84} - \frac{63}{84}$	=	$\frac{50}{84}$	=	$\frac{\frac{25}{42}}{\frac{1}{2}}$
4)	$\frac{12}{7} + \frac{18}{72} - \frac{20}{36} - \frac{7}{12} + \frac{5}{6} - \frac{2}{3} + \frac{7}{9} - \frac{3}{8}$	=			
	$\frac{864}{504} + \frac{126}{504} - \frac{280}{504} - \frac{294}{504} + \frac{420}{504} - \frac{336}{504} + \frac{392}{504} - \frac{189}{504}$	=			
	$\frac{1802}{504} - \frac{1099}{504} = \frac{703}{504} = \underline{1\frac{199}{504}}$				
5)	$3\frac{1}{2} + 4\frac{3}{5} - 6\frac{11}{14} + \frac{29}{35} - \frac{9}{10} + 2\frac{29}{35} + 1\frac{3}{7}$	=			
	$\frac{7}{2} + \frac{23}{5} - \frac{95}{14} + \frac{29}{35} - \frac{9}{10} + \frac{99}{35} + \frac{10}{7}$	=			
	$\frac{245}{70} + \frac{322}{70} - \frac{475}{70} + \frac{58}{70} - \frac{63}{70} + \frac{198}{70} + \frac{100}{70}$	=			
	$\frac{923}{70} - \frac{538}{70} = \frac{385}{70} = 5\frac{35}{70} = 5\frac{1}{2}$				
6)	$\frac{432}{576} \cdot \frac{95}{133} = \frac{108}{144} \cdot \frac{5}{7} = \frac{27}{36} \cdot \frac{5}{7} = \frac{3}{4} \cdot \frac{5}{7} =$	$\frac{15}{28}$	=		
7)	$\frac{41}{118} \cdot \frac{59}{205} = \frac{1}{2} \cdot \frac{1}{5} = \frac{1}{10}$				
8)	$\frac{81}{243} \cdot \frac{27}{18} = \frac{1}{3} \cdot \frac{1}{2} = \frac{1}{1} \cdot \frac{1}{2} = \frac{1}{2}$				
9)	$\frac{32}{64} \cdot \frac{17}{49} \cdot \frac{13}{11} \cdot \frac{98}{17} \cdot \frac{22}{39} \cdot \frac{33}{77} \cdot \frac{16}{64} = \frac{1}{2} \cdot \frac{17}{49} \cdot \frac{13}{11} \cdot \frac{98}{17} \cdot \frac{22}{39}$ $\frac{1}{2} \cdot \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{2}{1} \cdot \frac{2}{3} \cdot \frac{3}{7} \cdot \frac{1}{4} = \frac{1}{2} \cdot \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{1}{3} \cdot \frac{3}{42} = \frac{1}{14}$	$\frac{3}{7}$ $\frac{3}{7}$	$\cdot \frac{1}{4}$ $\frac{1}{1}$	=	



$$\begin{aligned} \mathbf{10} \quad \frac{15}{46} \cdot \frac{126}{414} \cdot \frac{23}{10} \cdot \frac{2317}{4011} \cdot \frac{21}{2317} \cdot \frac{21}{27} &= \frac{15}{46} \cdot \frac{63}{207} \cdot \frac{23}{10} \cdot \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{7}{9} &= \frac{3}{2} \cdot \frac{7}{23} \cdot \frac{1}{2} \cdot \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{7}{9} &= \frac{1}{2} \cdot \frac{7}{23} \cdot \frac{1}{2} \cdot \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{7}{3} &= \frac{47}{276} \\ \mathbf{11} \quad 3\frac{3}{4} \cdot 4\frac{7}{9} &= \frac{15}{4} \cdot \frac{43}{9} &= \frac{5}{4} \cdot \frac{43}{3} &= \frac{215}{12} &= \frac{17\frac{11}{12}}{12} \\ \mathbf{12} \quad 6\frac{4}{7} \cdot 5\frac{11}{23} &= \frac{46}{7} \cdot \frac{1226}{23} &= \frac{2}{1} \cdot \frac{18}{1} &= \frac{36}{18} \\ \mathbf{13} \quad 2\frac{1}{3} \cdot 5\frac{5}{6} &= \frac{7}{3} \cdot \frac{25}{6} &= \frac{245}{18} &= \frac{13\frac{11}{18}}{18} \\ \mathbf{14} \quad 1\frac{8}{17} \cdot 1\frac{38}{117} \cdot 6\frac{4}{5} \cdot 1\frac{8}{31} &= \frac{25}{17} \cdot \frac{155}{117} \cdot \frac{34}{5} \cdot \frac{39}{31} &= \frac{5}{16} \cdot \frac{5}{3} \cdot \frac{2}{1} \cdot \frac{1}{1} &= \frac{50}{53} &= \frac{16\frac{2}{3}}{16} \\ \mathbf{15} \quad \frac{2}{3} \cdot \frac{4}{5} &= \frac{2}{3} \cdot \frac{5}{4} &= \frac{1}{3} \cdot \frac{5}{2} &= \frac{5}{6} \\ \mathbf{16} \quad \frac{4}{5} \cdot \frac{2}{3} &= \frac{9}{11} \cdot \frac{77}{36} &= \frac{1}{1} \cdot \frac{7}{4} &= \frac{1\frac{3}{4}}{\frac{4}{5}} \\ \mathbf{18} \quad \left(\frac{12}{16} \cdot \frac{54}{81}\right) \cdot \left(\frac{48}{114} \cdot \frac{24}{798}\right) &= \left(\frac{3}{4} \cdot \frac{2}{3}\right) \cdot \left(\frac{8}{19} \cdot \frac{13}{133}\right) &= \left(\frac{3}{4} \cdot \frac{3}{2}\right) \cdot \left(\frac{8}{19} \cdot \frac{133}{4}\right) &= \frac{9}{8} \cdot \left(\frac{2}{1} \cdot \frac{7}{1}\right) &= \frac{9}{8} \cdot \frac{14}{1} &= \frac{9}{8} \cdot \frac{11}{1} &= \frac{9}{8} \cdot \frac{11}{1} \\ \mathbf{19} \quad \left(12\frac{1}{4} \cdot \frac{7}{1}\right) \cdot \left(3\frac{5}{6} \cdot 7\frac{7}{27}\right) &= \left(\frac{49}{4} \cdot \frac{7}{12}\right) \cdot \left(\frac{23}{6} \cdot \frac{196}{19}\right) &= \frac{21}{1} \cdot \frac{207}{207} &= \frac{21}{1} \cdot \frac{392}{207} \\ \frac{7}{1} \cdot \frac{392}{69} &= \frac{27444}{69} &= \frac{39\frac{53}{69} \\ \mathbf{19} \cdot \frac{19}{69} &= \frac{39\frac{53}{69}} \\ \mathbf{19} \cdot \frac{11}{69} &= \frac{39\frac{53}{69}} \\ \mathbf{11} \cdot \frac{392}{69} &= \frac{27444}{69} &= \frac{39\frac{53}{69}} \\ \mathbf{11} \cdot \frac{392}{69} &= \frac{39\frac{53}{69}} \\ \mathbf$$



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$$\begin{aligned} \mathbf{20} \quad \frac{29}{3} + \frac{4}{6} \cdot \frac{5}{10} \cdot \frac{125}{625} - \frac{103}{515} \cdot \frac{67}{31} \cdot \frac{62}{268} &= \frac{29}{3} + \frac{2}{3} \cdot \frac{1}{2} \cdot \frac{1}{5} - \frac{1}{5} \cdot \frac{1}{1} \cdot \frac{2}{4} &= \\ \frac{29}{3} + \frac{2}{30} - \frac{2}{20} &= \frac{29}{3} + \frac{1}{15} - \frac{1}{10} &= \frac{290}{30} + \frac{2}{30} - \frac{3}{30} &= \frac{289}{30} &= \frac{9\frac{19}{30}}{30} \end{aligned}$$

$$\begin{aligned} \mathbf{21} \quad \left(4\frac{7}{12} - 2\frac{1}{6}\right) \cdot \left(3\frac{5}{9} - 2\frac{3}{4}\right) + \frac{39}{72} : 1\frac{5}{8} &= \left(\frac{55}{12} - \frac{13}{6}\right) \cdot \left(\frac{32}{9} - \frac{11}{4}\right) + \frac{13}{24} : \frac{13}{8} &= \\ \left(\frac{55}{12} - \frac{26}{3}\right) \cdot \left(\frac{128}{36} - \frac{99}{36}\right) + \frac{13}{24} \cdot \frac{8}{13} &= \frac{29}{12} \cdot \frac{29}{36} + \frac{1}{3} \cdot \frac{1}{1} &= \\ \frac{841}{432} + \frac{144}{432} &= \frac{985}{432} &= 2\frac{121}{432} \end{aligned}$$

$$\begin{aligned} \mathbf{22} \left(1\frac{2}{3}:4\frac{1}{2}\right)^3 + 7\frac{1}{4}\cdot 3\frac{5}{9} - 4\frac{17}{36} + \left(1\frac{1}{2}\right)^5 &= \left(\frac{5}{3}:\frac{9}{2}\right)^3 + \frac{29}{4}\cdot \frac{32}{9} - \frac{161}{36} + \left(\frac{3}{2}\right)^5 &= \\ \left(\frac{5}{3}\cdot\frac{2}{9}\right)^3 + \frac{928}{36} - \frac{161}{36} + \frac{243}{32} &= \left(\frac{10}{27}\right)^3 + \frac{137}{36} + \frac{243}{32} &= \\ \frac{1000}{19638} + \frac{137}{36} + \frac{243}{32} &= \frac{32000}{629856} + \frac{2396952}{629856} + \frac{4782969}{629856} &= \\ \frac{7211921}{629856} &= 11\frac{233505}{629856} &= \\ 11\frac{25945}{69984} &= \end{aligned}$$

$$23) \ 15\frac{2}{3} - \left[6\frac{1}{2}\left(2\frac{1}{4} - \frac{7}{8}\right) + \frac{3}{4}\right] \cdot \frac{1}{6} = \frac{47}{3} - \left[\frac{13}{2}\left(\frac{18}{8} - \frac{7}{8}\right) + \frac{3}{4}\right] \cdot \frac{1}{6} = \frac{47}{3} - \left[\frac{13}{2} \cdot \frac{11}{8} + \frac{12}{16}\right] \cdot \frac{1}{6} = \frac{47}{3} - \frac{155}{16} \cdot \frac{1}{6} = \frac{1504}{96} - \frac{155}{96} = \frac{1349}{96} = \frac{14\frac{5}{96}}{16}$$

$$24) \left(3\frac{1}{8} - 2\frac{3}{4}\right)^{2} + \frac{5}{2} + \frac{3}{8} + \frac{1}{2}\left(\frac{3}{2} \cdot \frac{6}{8}\right)^{2} = \left(\frac{25}{8} - \frac{22}{8}\right)^{2} + \frac{20}{8} + \frac{3}{8} + \frac{1}{2}\left(\frac{3}{2} \cdot \frac{8}{6}\right)^{2} = \left(\frac{3}{8}\right)^{2} + \frac{23}{8} + \frac{1}{2}\left(\frac{1}{1} \cdot \frac{4}{2}\right)^{2} = \frac{9}{64} + \frac{184}{64} + \frac{1}{2} \cdot 4 = \frac{193}{64} + 2 = \frac{5\frac{1}{64}}{164}$$



$$25) \quad 12 \cdot 14 - 7\frac{1}{2} \cdot 5 + 6\frac{1}{3} \cdot \left(3 - \frac{1}{2}\right)^3 = 168 - \frac{15}{2} \cdot \frac{5}{1} + \frac{19}{3} \cdot \left(\frac{5}{2}\right)^3 = 168 - \frac{15}{2} \cdot \frac{5}{1} + \frac{19}{3} \cdot \left(\frac{5}{2}\right)^3 = 168 - \frac{75}{2} + \frac{19}{3} \cdot \frac{125}{8} = \frac{4032}{24} - \frac{900}{24} + \frac{2375}{24} = \frac{5507}{24} = 229\frac{11}{24}$$





